

Tutorial 3

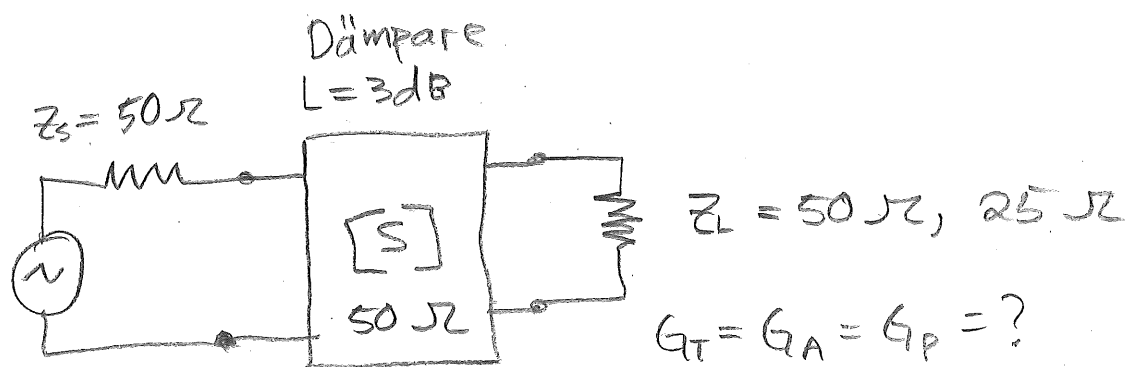
Agenda

- * Stability
- * Unilateral design ($S_{12} \approx 0$)
- * Bilateral design ($S_{12} \neq 0$)

Glöm ej

- Räkna uppgifterna själva $\rightarrow$ see att det blir rätt
- Finns mängder av gamla tentatal

P. 6,3



Dämpare = passiv reciprok device

inga reflektioner

$$[S] = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} = \begin{bmatrix} 0 & 0,708 \\ 0,708 & 0 \end{bmatrix}$$

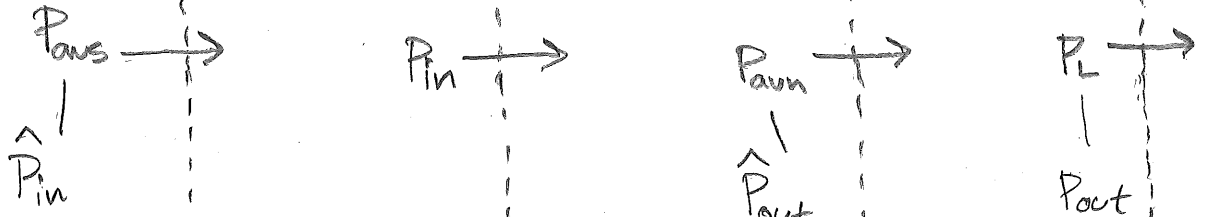
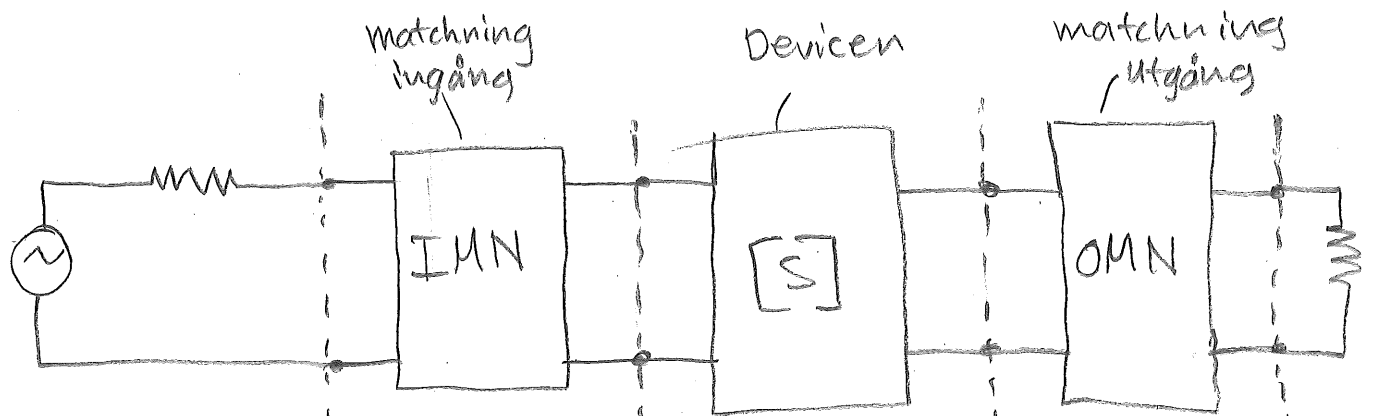
$$G = -3\text{dB} = |S_{21}|_{\text{dB}} = |S_{12}|_{\text{dB}} = 20\log|S_{21}|$$

$$\Rightarrow |S_{21}| = 10^{-\frac{3}{20}} =$$

$$= 0,708$$

$$\Rightarrow |S_{12}| = 0,708$$

↑
↑
samma transmission
i båda riktningarna



$$G_T = \frac{P_L}{P_{avs}} = \frac{P_{out}}{\hat{P}_{in}}$$

beror på IMN, OMN

$$G_P = \frac{P_L}{P_{in}} = \frac{P_{out}}{P_{in}}$$

beror på OMN

$$G_A = \frac{P_{avn}}{P_{avs}} = \frac{\hat{P}_{out}}{\hat{P}_{in}}$$

beror på IMN

$$G_T = \frac{|S_{21}|^2 (1 - |\Gamma_s|^2) (1 - |\Gamma_L|^2)}{|1 - \Gamma_s \Gamma_{in}|^2 |1 - S_{22} \Gamma_L|^2}$$

P 6,16

$$\Gamma_L = ? \quad \Gamma_s = ?$$

$$\Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0} = 0 = \Gamma_s$$

50 50

$$\Gamma_s = \Gamma_L = 0$$

$$\Rightarrow G_T = |S_{21}|^2 = 0.708^2 = -3 \text{ dB}$$

$$G_P = \frac{|S_{21}|^2 (1 - |\Gamma_L|^2)}{(1 - |\Gamma_{in}|^2) |1 - S_{22} \Gamma_L|^2}$$

$$\Gamma_{in} = S_{11} + \frac{S_{12} S_{21} \Gamma_L}{1 - S_{22} \Gamma_L} = 0$$

=0 =0

P 6,11

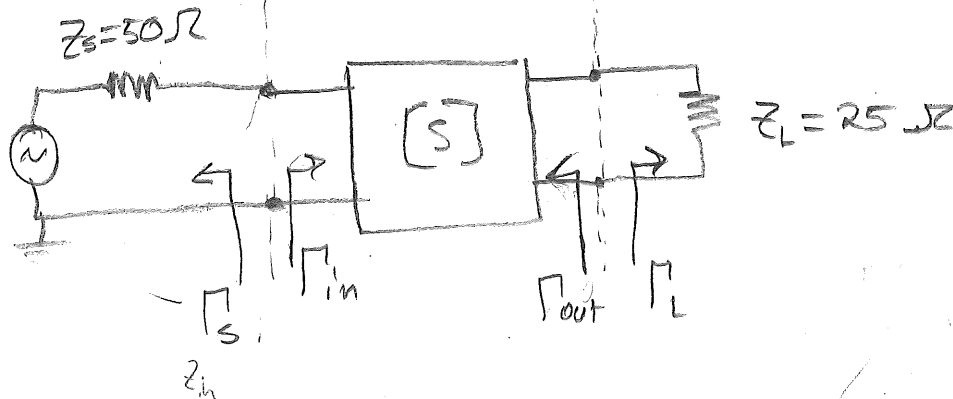
$$\Rightarrow G_P = |S_{21}|^2 = -3 \text{ dB}$$

$$G_A = \frac{|S_{21}|^2 (1 - |\Gamma_s|^2)}{|1 - S_{11} \Gamma_s|^2 (1 - |\Gamma_{out}|^2)} - P. 6,15$$

$$\Gamma_{out} = \frac{Z_{out} - Z_L}{Z_{out} + Z_L} = 0$$

$$\Rightarrow G_A = |S_{21}|^2 = -3 \text{ dB}$$

$$\underline{Z_L = 25 \Omega} \quad Z_L / Z_0$$



$$\underline{G_T}: \Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{25 - 50}{25 + 50}$$

$$\Gamma_s = \frac{Z_s - Z_0}{Z_s + Z_0} = 0$$

$$\Rightarrow \Gamma_L = -1/3$$

$$\Gamma_{in} = S_{11} + \frac{S_{12} S_{21} \Gamma_L}{1 - S_{22} \Gamma_L} =$$

$$= 0$$

$$\neq S_{11} + S_{12} S_{21} \Gamma_L = 0,708^2 \cdot -1/3 = -1/6$$

$$G_T = \dots = 0,4456 \text{ (beror på } Z_L, Z_s)$$

$$G_A = \dots = 0,501 = -3 \text{ dB (beror ej på } Z_L)$$

$$G_P = \dots = 0,458 \text{ (beror på } Z_L)$$

6.4 $f = 1,8 \text{ GHz}$ $S = \begin{bmatrix} 0,34 \angle -77^\circ & 0,06 \angle 70^\circ \\ 4,3 \angle 80^\circ & 0,45 \angle -25^\circ \end{bmatrix}$

$K = ?$ $\mu = ? \rightarrow$ stability circles

K- Δ test P. 6,31-32

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{12}S_{21}|} = \dots = 1,35 > 1 \text{ ok}$$

$\swarrow \Rightarrow$ stable

$$|\Delta| = |S_{11}S_{22} - S_{12}S_{21}| = 0,1177 < 1$$

μ -test P 6,33

$$\mu = \frac{1 - |S_{11}|^2}{|S_{22} - \Delta S_{11}^*| + |S_{12}S_{21}|} = \dots = \underline{1,193} > 1 \Rightarrow \underline{\text{stable}}$$

6,9 Design max gain amplifier

$f = 5 \text{ GHz}$ Transistor: GaAs FET

$$Z_0 = 50 \Omega$$

$$[S] = \begin{bmatrix} 0,65 \angle -140^\circ & 0,04 \angle 60^\circ \\ 2,4 \angle 50^\circ & 0,70 \angle -65^\circ \end{bmatrix}$$

For matching: use Open circuit for IMN , OMN

1. Är transistoren stabil?

K-Δ P 6,37-32

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{12}S_{21}|} = \dots = 1,260371$$

$$|\Delta| = |S_{11}S_{22} - S_{12}S_{21}| = \dots = 0,393 < 1$$

$$\left. \begin{array}{l} K = \dots \\ |\Delta| = \dots \end{array} \right\} \Rightarrow \text{stabil}$$

2. Kan vi tillämpa unilateral design?
→ annars bilateral

* Angärs av S_{12} , kolla $U =$ "Ett mått på hur unilateral vår device är"

$$U = \frac{|S_{11}| |S_{12}| |S_{21}| |S_{22}|}{(1 - |S_{11}|^2)(1 - |S_{22}|^2)} = \frac{1}{1 - G_T} = \frac{1}{1 - 0,05} = 0,1483 > 0,05$$

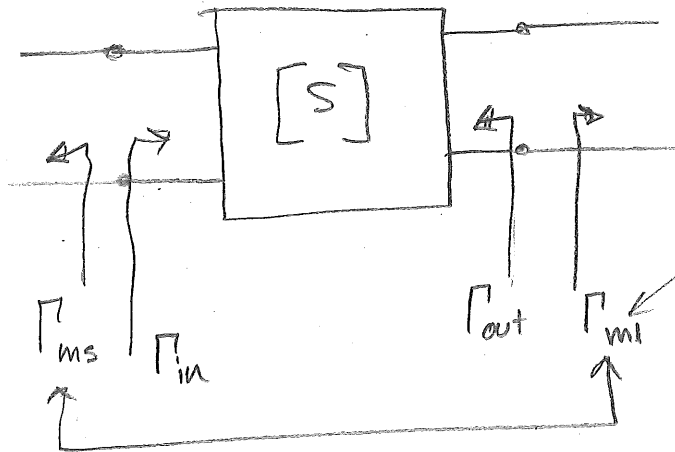
our rule of thumb
↓

$$\frac{1}{(1-u)^2} = 1,38 = 1,394 \text{ dB}$$

för stort fel $\rightarrow$

3. Tillämpa unilateral eller bilateral design vårt fall

- Vi har tärddiga formuler för max gain
för bilateral design



Förmlerna bestämmer konjugatreflektionskoefficienterna

d.v.s. $\Gamma_{ms} = \Gamma_{in}^*$ $\Gamma_{ml} = \Gamma_{out}^*$
 $(Z_s = Z_{in}^*)$

Pozar 6.43 --- 44

$$\Gamma_{ms} = \frac{B_1 \pm \sqrt{B_1^2 - 4|C_1|^2}}{2C_1}$$

$$\Gamma_{ml} = \frac{B_2 \pm \sqrt{B_2^2 - 4|C_2|^2}}{2C_2}$$

$$B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2$$

$$B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2$$

$$\Delta = S_{11}S_{22} - S_{12}S_{21}$$

$$C_1 = S_{11} - \Delta S_{22}^*$$

$$C_2 = S_{22} - \Delta S_{11}^*$$

$$\Rightarrow \Gamma_{ml} = \dots = 0,85 \angle 71^\circ$$

$$\Gamma_{ms} = \dots = 0,83 \angle 147^\circ$$

Nu kan vi beräkna gainet (anta transducer gain G_T om inget annat anges)

P. 6.16

$$G_T = \frac{(1 - |\Gamma_s|^2)}{|1 - \Gamma_s \Gamma_{in}|^2} \cdot \frac{|S_{21}|^2 (1 - |\Gamma_L|^2)}{|1 - S_{22} \Gamma_L|^2}$$

$G_s = 3.14$ $G_o = 5.76$ $G_L = 1.64$

kolla i boken för unilaterala tallet

$\Gamma_s = \Gamma_{ms}$
 $\Gamma_L = \Gamma_{ml}$
 $\Gamma_{in} = \Gamma_{ms}^*$

P. 6.22a

$$\Gamma_{in} = \frac{S_{11} + S_{12} S_{21} \Gamma_L}{1 - S_{22} \Gamma_L} = \dots = 0.83 \angle -147^\circ = \Gamma_{ms}^* \text{ ok!}$$

$$\Rightarrow G_T = \dots = 29.6 = 14.7 \text{ dB}$$

4. Matchningsdät

skapa $\Gamma_{ms} = 0.83 \angle 147^\circ$

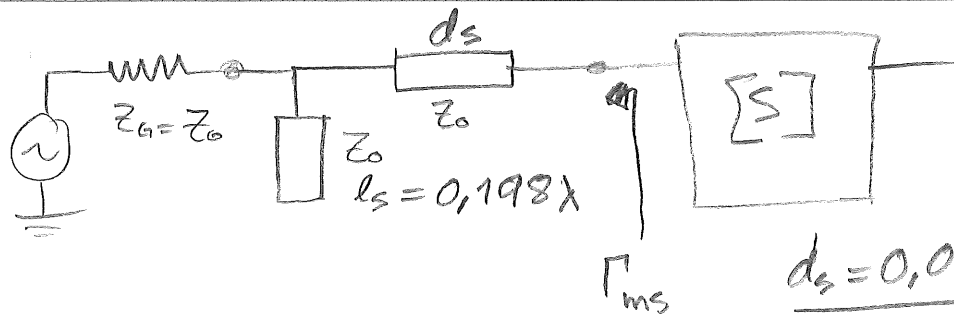
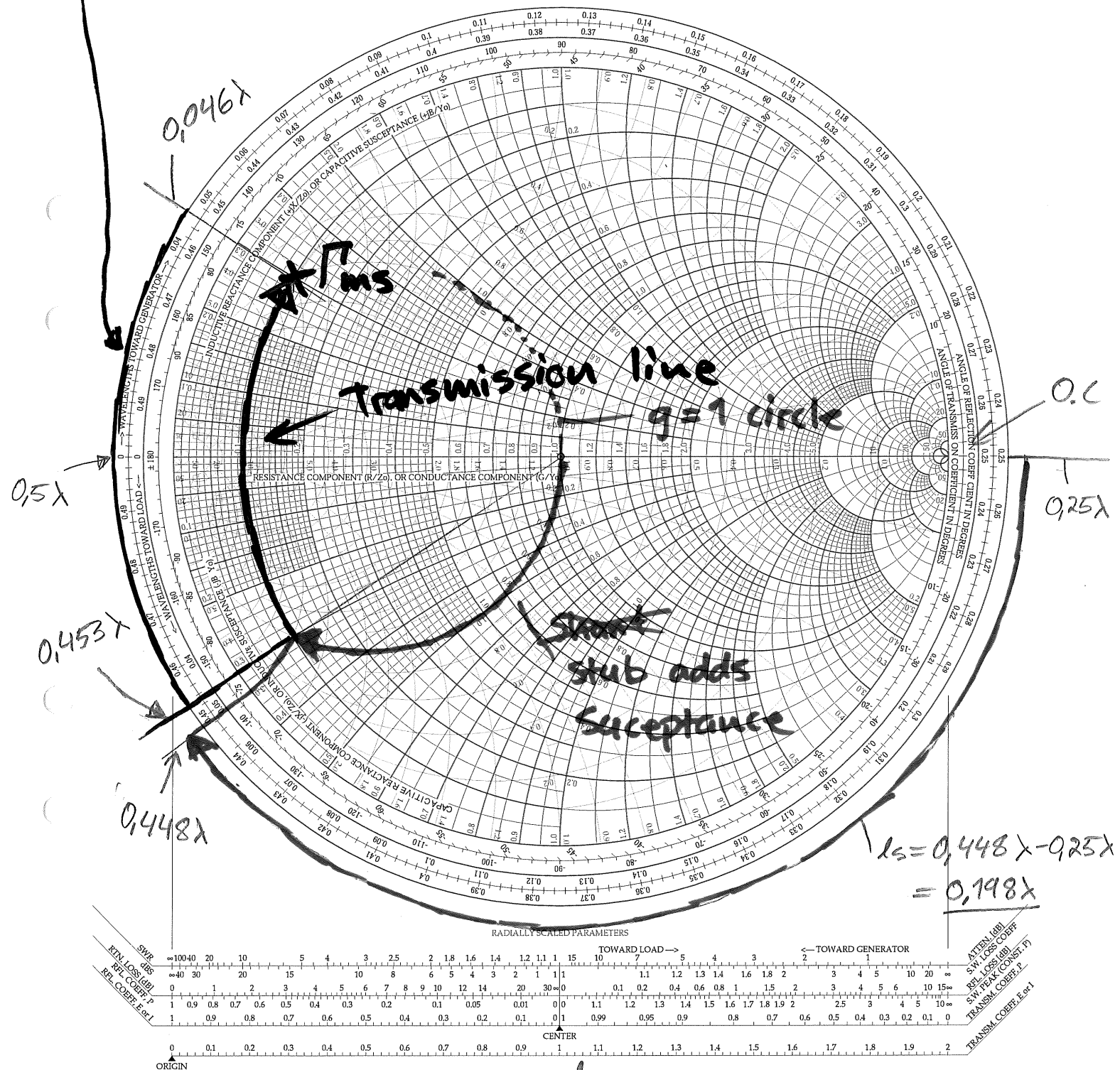
1. Markera Γ_{ms}
2. Dra Γ_{ms} cirkeln så att du skär $g=1$ cirkeln
3. Lägg till stubben så att du hamnar på Γ_{ms} cirkeln. Bestäm l_s
4. Roter med transmissionsledning till Γ_{ms} . Bestäm längden på ledningen d_s

Γ_{ms}

$$d_s = 0,5\lambda - 0,453\lambda + 0,046\lambda = 0,093\lambda$$

NAME	TITLE	DWG. NO.
SMITH CHART FORM ZY-01-N	Microwave Circuit Design - EE523 - Fall 2000	DATE

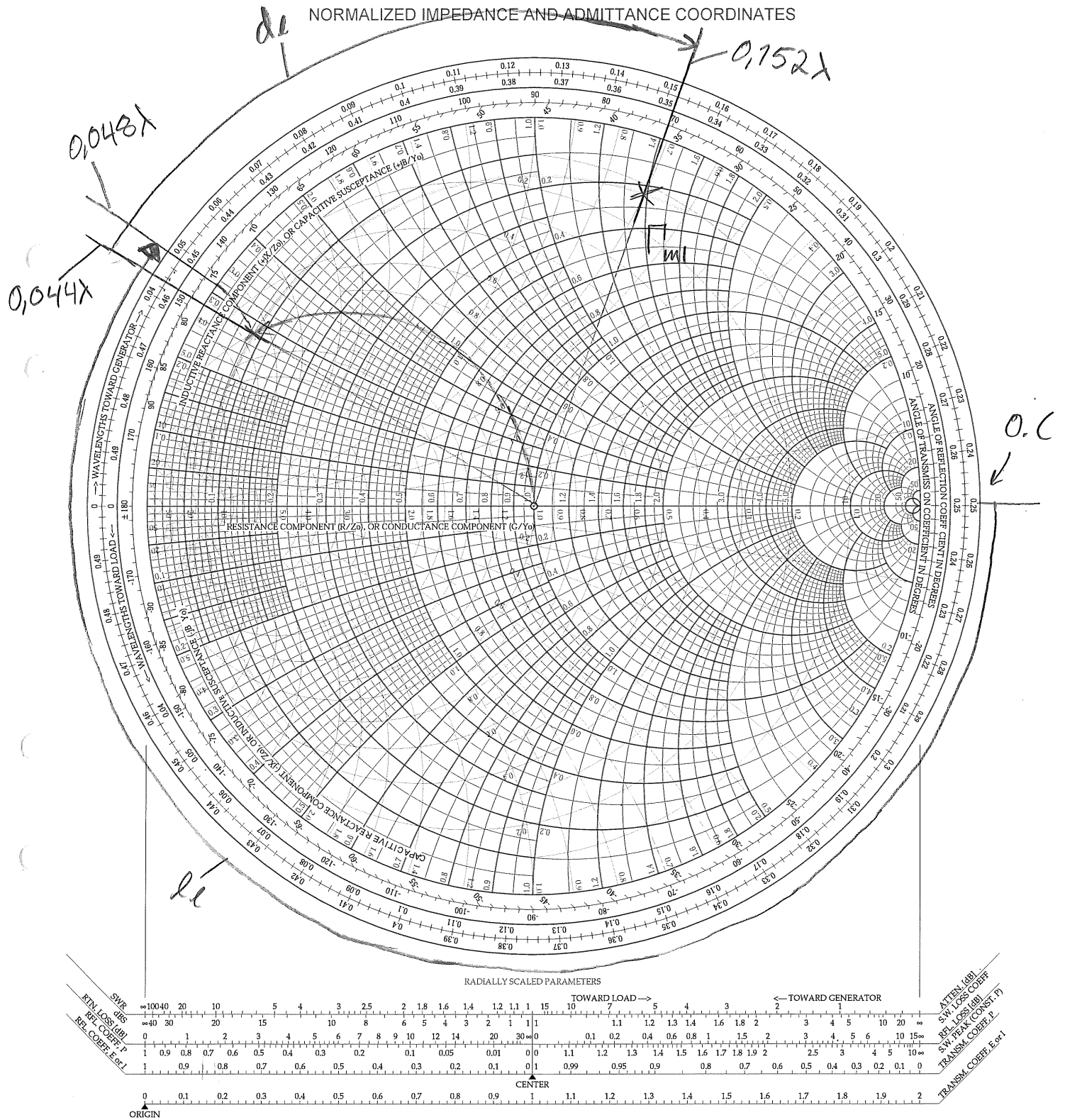
NORMALIZED IMPEDANCE AND ADMITTANCE COORDINATES



R_{in}

$$d_e = 0,152\lambda - 0,044\lambda = \underline{0,108\lambda}$$

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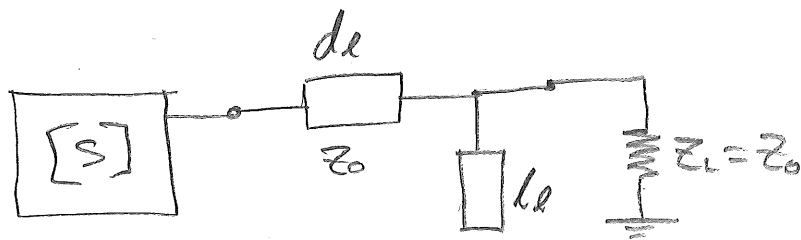


$$d_i = 0,25\lambda + 0,048\lambda = \underline{0,298\lambda}$$

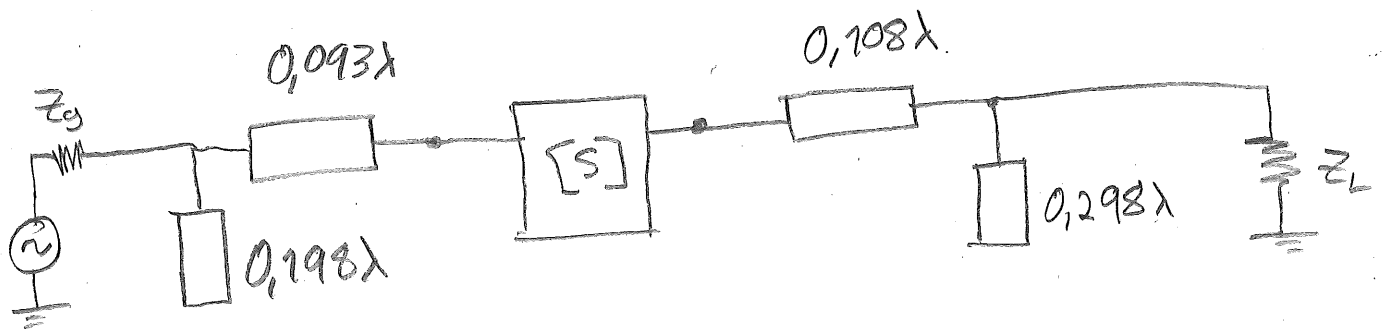
$$\Gamma_{in} = 0,85 \angle 71^\circ$$

$$d_e = 0,108\lambda$$

$$\text{ samma procedur } \Rightarrow l_e = 0,298\lambda$$



vi har nu hela designen:



Tenta 170411 3

Från uppg 2 bestämde vi: $\Gamma_s = 0,9 \angle -90^\circ$
 $\Gamma_L = 0,5 \angle -180^\circ$

För transistorn: $[S] = \begin{bmatrix} 0,8 \angle 90^\circ & 0,01 \angle 90^\circ \\ 5 \angle 0^\circ & 0,9 \angle 0^\circ \end{bmatrix}$

Finns det något problem?

→ Kolla stabilitet P. 6,31 (K- Δ , rollets)

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{12}S_{21}|} = < 1 \quad \dots \quad \overset{P 6,33}{M} = \dots = 0,87 < 1$$

$$|\Delta| = |S_{11}S_{22} - S_{12}S_{21}| =$$

∴ pot. instabil

Rita stabilitetscirklar på ingång och utgång

P. 6,28-29

$$C_L = \frac{(S_{22} - \Delta S_{11}^*)^*}{|S_{22}|^2 - |\Delta|^2} = \dots = 1,01$$

$$R_L = \left| \frac{S_{12} S_{21}}{|S_{22}|^2 - |\Delta|^2} \right| = \dots = 0,14$$

Rita i S.D

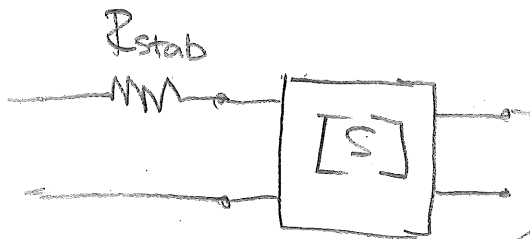
$$C_S = \frac{(S_{11} - \Delta S_{22}^*)^*}{|S_{11}|^2 - |\Delta|^2} = \dots = 1,03 \angle -90^\circ$$

$$R_S = \left| \frac{S_{12} S_{21}}{|S_{11}|^2 - |\Delta|^2} \right| = \dots = 0,26$$

- $S_{11} < 1 \Rightarrow$ cirkelns område = instabilt
- $\Gamma_S = 0,9 \angle -90^\circ$ ligger i instabilt område!
- b)
- Stabilisera med serieresistans på ingång

$$\Gamma = 0,3 \Rightarrow R_{stab} = \Gamma \cdot Z_0 = 0,3 \cdot 50 = \underline{15 \Omega}$$

viktigt!
labben etc



P. 6,46

$$G_{Tmax} = \frac{|S_{21}|}{|S_{12}|} \left(k - \sqrt{k^2 - 1} \right) = \frac{|S_{21}|}{|S_{12}|}$$

G_{msg}

$$= \frac{5}{0,01} = \underline{27 dB}$$

blir mindre då
 $k \nearrow$ alltså
 överstabilisering
 reducerar gain.
 Max gain då
 $k=1$ (precis stabil)

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