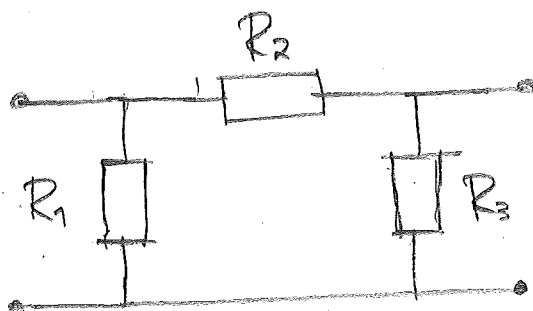
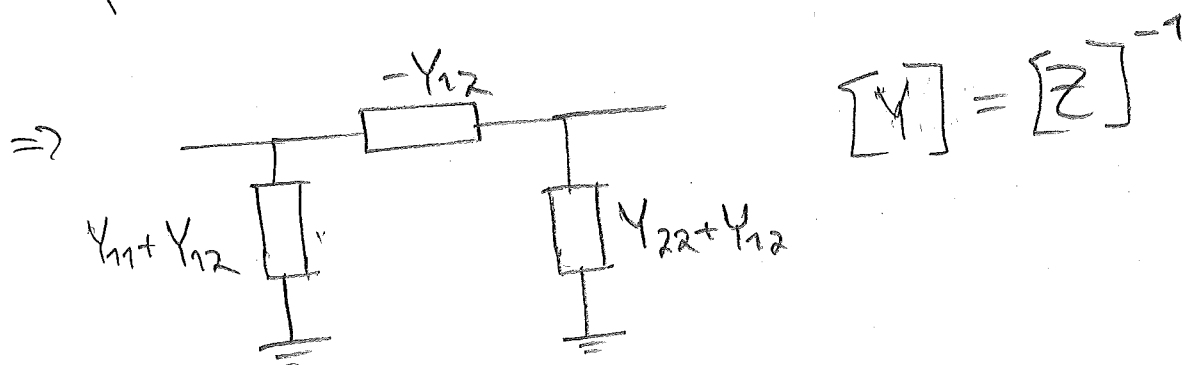


K3

$$\underline{Z} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} = \begin{bmatrix} 250 & 50 \\ 50 & 150 \end{bmatrix}$$



* Ett Π -schema, föreläsning 4 sid 14
(kommer finnas i tesen)



* Använd tabell 4,2 (kommer finnas i tesen)

* Vi kan också göra inverteringen

Tabell:

$$Y_{11} = \frac{Z_{22}}{|Z|} \quad |Z| = Z_{11}Z_{22} - Z_{12}Z_{21} =$$
$$= 250 \cdot 150 - 50^2 = 35000$$

$$= \frac{150}{35000}$$

$$Y_{12} = \frac{-Z_{12}}{|Z|} = \frac{50}{35000}$$

$$Y_{21} = \frac{-Z_{21}}{|Z|} = \frac{50}{35000}$$

$$Y_{22} = \frac{Z_{11}}{|Z|} = \frac{250}{35000}$$

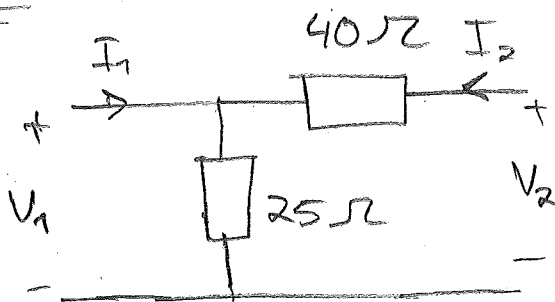
K3 forts

$$Y_{R1} = Y_{11} + Y_{12}, \quad R_1 = \frac{1}{Y_{R1}} = \underline{\underline{350 \Omega}}$$

$$Y_{R2} = -Y_{12}, \quad R_2 = \frac{1}{Y_{R2}} = \underline{\underline{700 \Omega}}$$

$$Y_{R3} = Y_{22} + Y_{12}, \quad R_3 = \frac{1}{Y_{R3}} = \underline{\underline{175 \Omega}}$$

K4

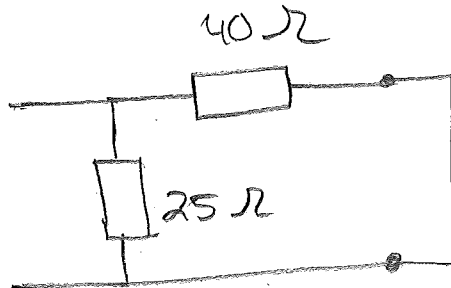


a) $Z_{22} = ?$

$$Z_{22} = \left. \frac{V_2}{I_2} \right|_{I_1=0} =$$

$$= 40 \Omega + 25 \Omega = \underline{\underline{65 \Omega}}$$

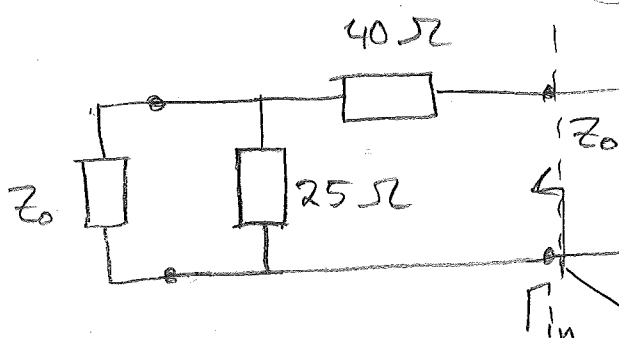
b) $Y_{11} = \left. \frac{I_1}{V_1} \right|_{V_2=0}$



$$= \frac{1}{25} + \frac{1}{40} = \underline{\underline{0,0650 \text{ S}}}$$

50 ohm terminering på port 1

c) $S_{22} = ? = \left. \frac{V_2^-}{V_2^+} \right|_{V_1^+ = 0}$



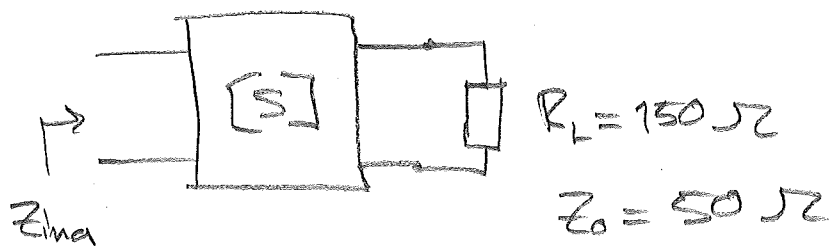
$$S_{22} = \Gamma_{in}$$

$$Z_{in} = \frac{Z_0 \cdot 25}{Z_0 + 25} + 40$$

$$\Gamma_{in} = \frac{Z_{in} - Z_0}{Z_{in} + Z_0} = -0,25$$

referensplanet

K8



$$S = \begin{bmatrix} 0,6 & 0,2 \\ 0,2 & 0,4 \end{bmatrix}$$

* konvertera $[S]$ till $[Z]$

Föreläsning 4 s 14, även handout + paper

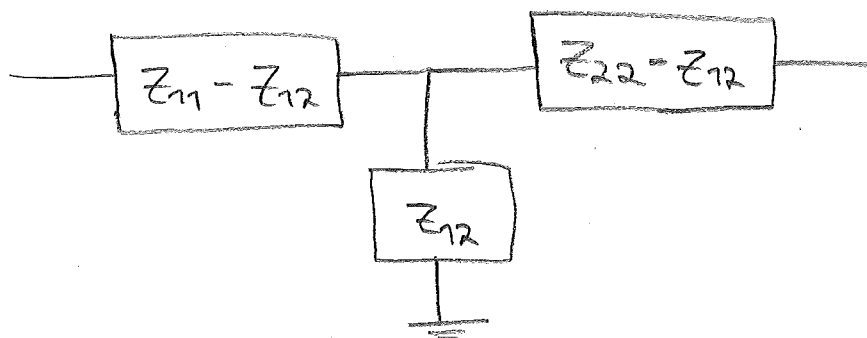


Table 4,2 (bland hjälpmedel pingpong)

$$Z_{11} = Z_0 \frac{(1-S_{11})(1-S_{22}) + S_{12}S_{21}}{(1-S_{11})(1-S_{22}) - S_{12}S_{21}} = \dots = 250 \Omega$$

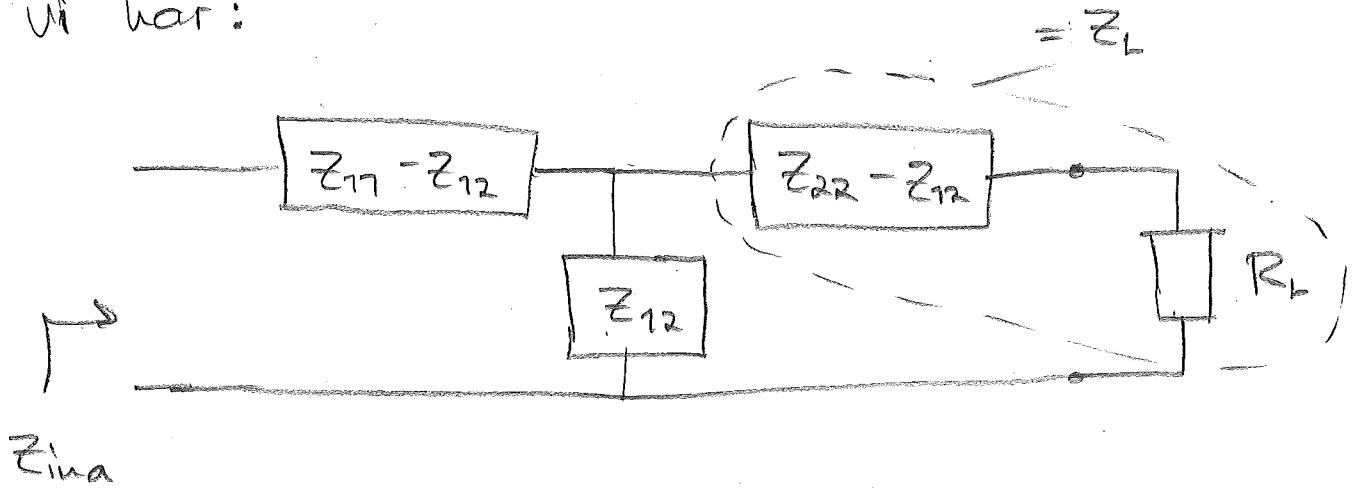
$$Z_{12} = Z_0 \frac{2S_{12}}{(1-S_{11})(1-S_{22}) - S_{12}S_{21}} = \dots = 100 \Omega$$

$$Z_{21} = Z_0 \frac{2S_{21}}{\dots} = \dots = 100 \Omega$$

$$Z_{22} = Z_0 \frac{(1-S_{11})(1+S_{22}) + S_{12}S_{21}}{(1-S_{11})(1-S_{22}) - S_{12}S_{21}} = \dots = 150 \Omega$$

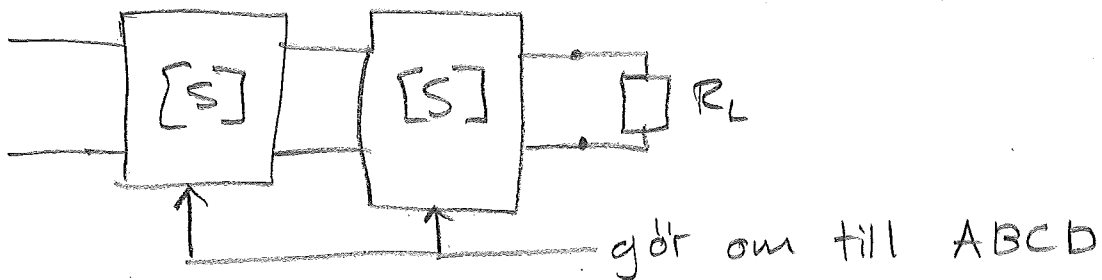
K8 torts

vi har:



$$Z_{ina} = z_{11} - z_{12} + \frac{z_L z_{12}}{z_L + z_{12}} = \dots = \underline{\underline{216,7 \Omega}}$$

b)



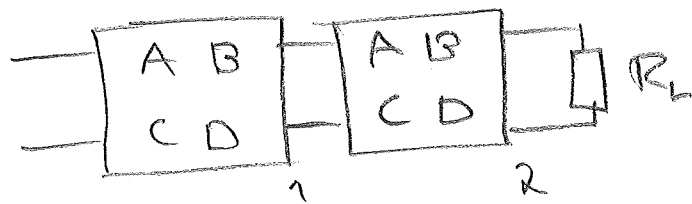
$$A = \frac{(1 + S_{11})(1 - S_{22}) + S_{12}S_{21}}{2S_{21}} = \dots = 2,5$$

$$B = Z_0 \frac{(1 + S_{11})(1 + S_{22}) - S_{12}S_{21}}{2S_{21}} = \dots = 275$$

$$C = \frac{1}{Z_0} \frac{(1 - S_{11})(1 - S_{22}) - S_{12}S_{21}}{2S_{21}} = \dots = 0,01$$

$$D = \frac{(1 - S_{11})(1 + S_{22}) + S_{12}S_{21}}{2S_{21}} = \dots = 1,5$$

K8 torts



multiplisera ihop

$$\begin{bmatrix} A_{\text{tot}} & B_{\text{tot}} \\ C_{\text{tot}} & D_{\text{tot}} \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 9 & 1100 \\ 0,04 & 5 \end{bmatrix}$$

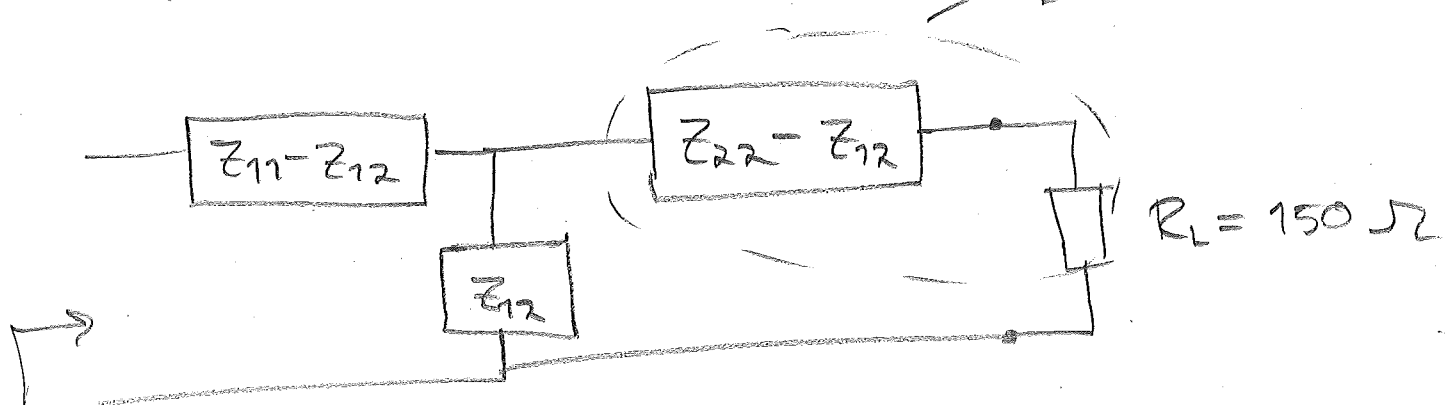
konvertera $\begin{bmatrix} & \\ & \end{bmatrix}_{ABCD} \rightarrow [Z]$

$$Z_{11} = A/C = 9/0,04 = 225 \quad Z_{12} = \frac{AD-BC}{C} = 25$$

$$Z_{21} = 1/C = 25 \quad Z_{22} = D/C = 125 \, \Omega$$

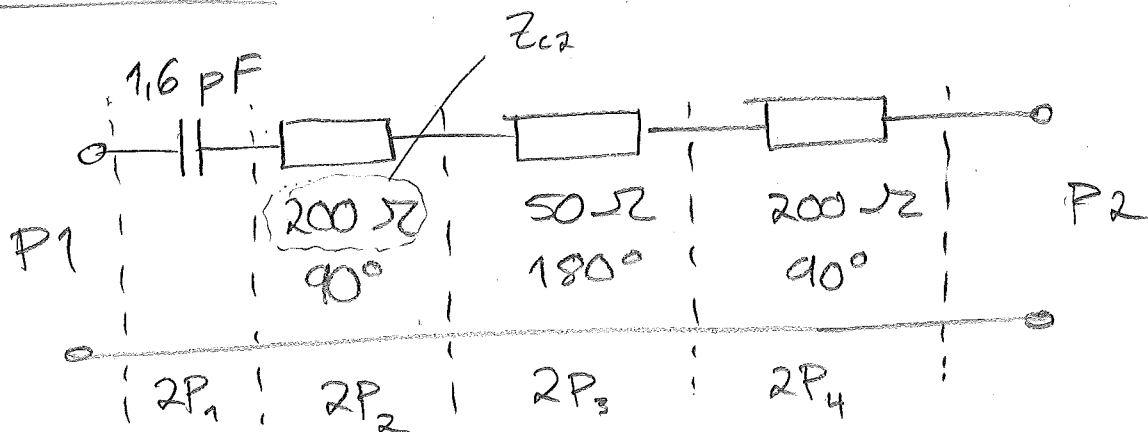
och vi får:

$$Z_L = Z_{22} - Z_{12} + R_L$$



Z_{inb}

$$Z_{inb} = Z_{11} - Z_{12} + \frac{Z_L Z_{12}}{Z_L + Z_{12}} = \dots = \underline{\underline{222,2 \, \Omega}}$$



* Flera 2 portar i kaskadkoppling

* Ta fram ABCD-matris för varje 2-port (används vid kaskadkoppl.)

* Multiplicera ihop alla ABCD-matriser

* Översätt totala ABCD-matrisen till S-parametrar

P. table 2.1

$$[2P_1]_{ABCD} = \boxed{Z_c} = \begin{bmatrix} 1 & Z_c \\ 0 & 1 \end{bmatrix} \quad Z_c = \frac{1}{j\omega C}$$

$$[2P_2]_{ABCD} = \begin{matrix} \xleftrightarrow{l} \\ \xleftrightarrow{Z_0} \\ \xleftrightarrow{l} \end{matrix} = \begin{bmatrix} \cos \beta l & jZ_0 \sin \beta l \\ jY_0 \sin \beta l & \cos \beta l \end{bmatrix} \quad \begin{matrix} Z_0 = Z_{c2} \\ Y_0 = Y_{c2} \end{matrix}$$

$$\beta l = \left\{ l = \frac{\lambda}{4} \right\} = \frac{2\pi}{\lambda} \cdot \frac{\lambda}{4} = \frac{\pi}{2} \quad \cos \frac{\pi}{2} = 0 \quad \sin \frac{\pi}{2} = 1$$

$$\Rightarrow [2P_2]_{ABCD} = \begin{bmatrix} 0 & jZ_{c2} \\ jY_{c2} & 0 \end{bmatrix}$$

$[2P_3]_{ABCD}$ = samme som innan
men $\frac{1}{2}$ nu

$$\beta l = \frac{2\pi}{\lambda} \cdot \frac{\lambda}{2} = \pi$$

$$\cos \pi = -1 \quad \sin \pi = 0$$

$$\Rightarrow [2P_3]_{ABCD} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$$

$$[2P_4]_{ABCD} = \text{Summa sum} = [2P_2]_{ABCD} = \begin{bmatrix} 0 & jZ_{C4} \\ jY_{C4} & 0 \end{bmatrix}$$

Nu totala ABCD

$$[2P]_{ABCD} = [2P_1][2P_2][2P_3][2P_4] =$$

$$= \begin{bmatrix} 1 & Z_c \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & jZ_{c2} \\ jY_{c2} & 0 \end{bmatrix} \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} 0 & jZ_{c4} \\ jY_{c4} & 0 \end{bmatrix} =$$

$$= \begin{bmatrix} Y_{C4} Z_{C2} & -jY_{C2} Z_{C4} / (C \cdot \omega) \\ 0 & Y_{C2} Z_{C4} \end{bmatrix} = \begin{bmatrix} 1 & -j99,5 \\ 0 & 1 \end{bmatrix}$$

Använd tabell i föreläsning 4 s 24

(kommer finnas i tentatesen)

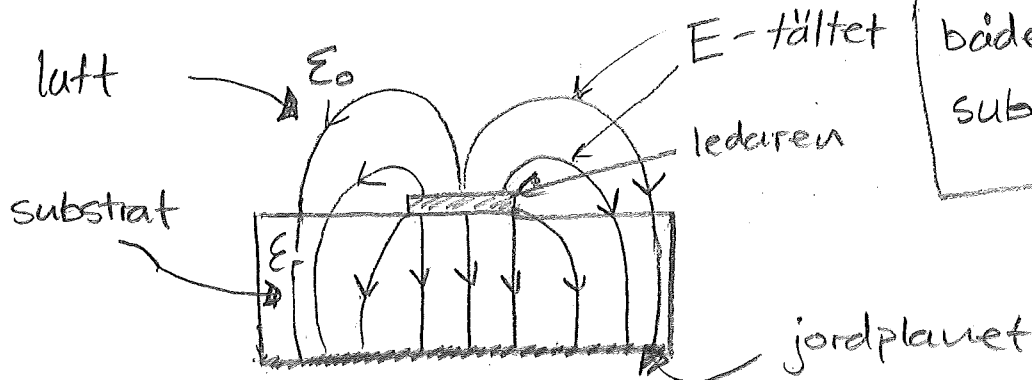
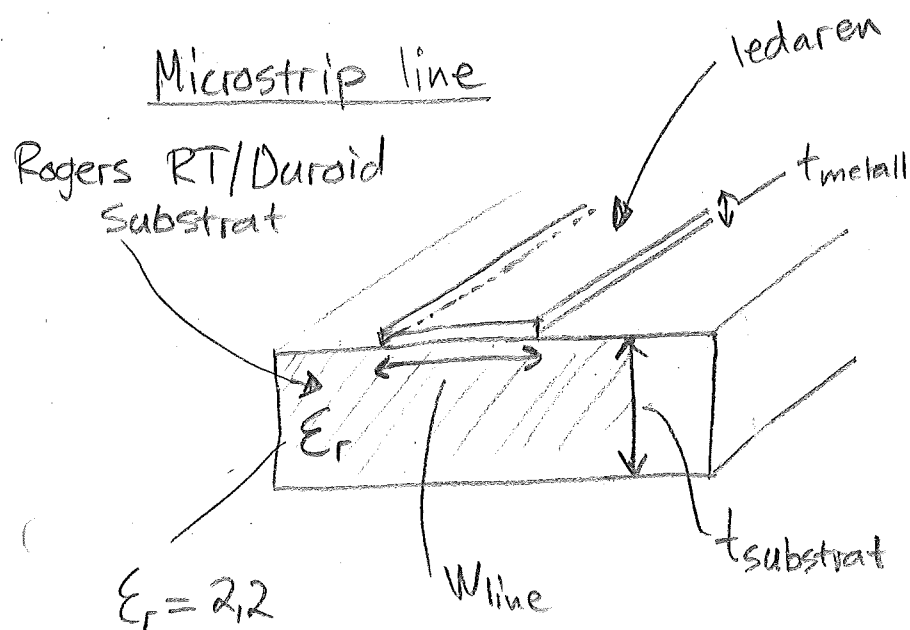
170411 1b forts

$$S_{11} = \frac{A + B/z_0 - C z_0 - D}{A + \frac{B}{z_0} + C z_0 + D} = \frac{1 - j100/50 - 0.50 - 1}{1 - j100/50 + 0.50 + 1} = \underline{\underline{0,705 \angle -45,2^\circ}}$$

$$S_{12} = \frac{2(AD - BC)}{A + B/z_0 + C z_0 + D} = \dots = \underline{\underline{0,709 \angle 44,8^\circ}}$$

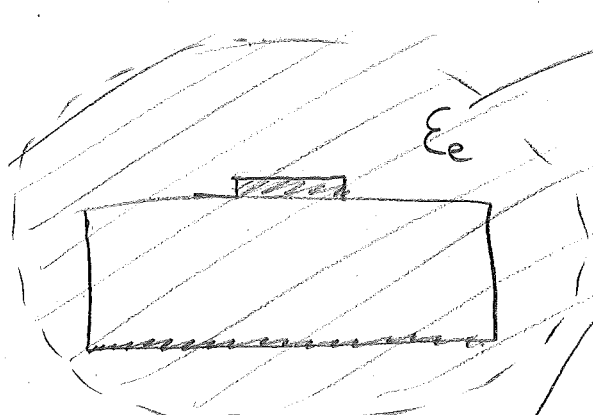
$$S_{21} = \frac{2}{A + B/z_0 + C z_0 + D} = \dots = \underline{\underline{0,709 \angle 44,8^\circ}}$$

$$S_{22} = \frac{-A + B/z_0 - C z_0 + D}{A + B/z_0 + C z_0 + D} = \dots = \underline{\underline{0,705 \angle -45,2^\circ}}$$



(vågorna)
Fältet utbreder sig i både luften och i substratet

Vi får en viktning mellan ϵ_0 och ϵ_r den effektiva permittiviteten blir ϵ_e



Effektiva permittiviteten våglängden i ϵ_e ?

→ $\lambda_{\text{quasi, TEM}}$

kallas kvasi TEM våglängden

och det är den vi hittar

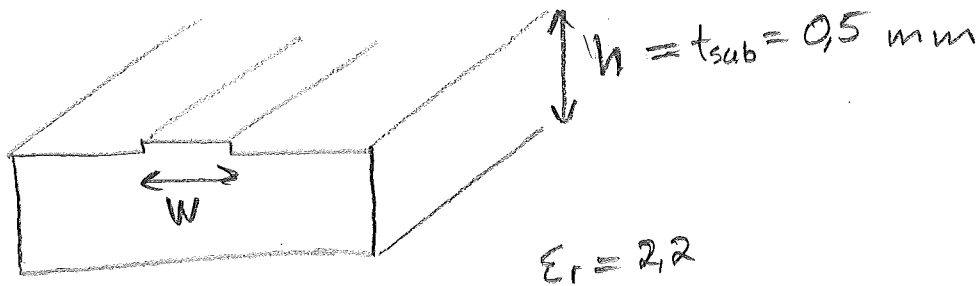
i våra diagram



våglängden i ϵ_e



våglängden i substratet ϵ_r



$$l_{bias} = 18,6 \text{ mm}, \quad l_s = 2,8 \text{ mm}, \quad l_e = 10 \text{ mm}$$

$$d_s = 24,5 \text{ mm} \quad d_e = 6,1 \text{ mm}$$

$$W_{bias} = 0,8 \text{ mm} \quad W_{lines} = 1,6 \text{ mm} \quad C = 100 \text{ pF}$$

a) $Z_{0, line} = ?$ $Z_{0, bias} = ?$ * använd diagram

bias

$$\frac{W}{h} = \frac{0,8}{0,5} = 1,6 \Rightarrow Z_0 = 70 \Omega$$

75 ←
50 ← } facit

Lines

$$\frac{W}{h} = \frac{1,6}{0,5} = 3,2 \Rightarrow Z_0 = 45 \Omega$$

lös av från diagram

b) $\frac{\lambda}{\lambda_{TEM}} = \frac{\lambda \sqrt{\epsilon_r}}{\lambda_0} = 1,075 \quad (1)$

← kvasi tem

↑
vanlig TEM

i homogent material

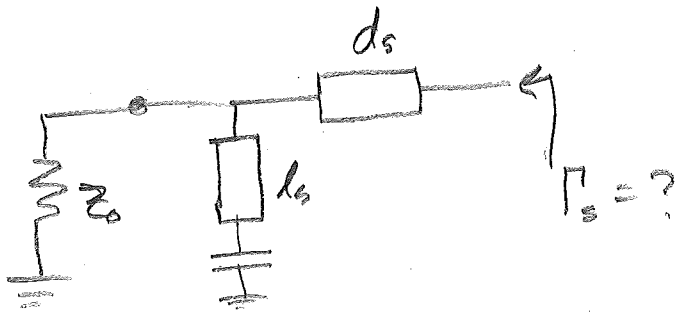
biasledning

$$\frac{\lambda}{4} = 18,6 \text{ mm} \Rightarrow \lambda = 74,4 \text{ mm}$$

$$(1) \Rightarrow \lambda_0 = \frac{74,4 \sqrt{\epsilon_r}}{1,075} \text{ mm} = 102,65 \text{ mm} \quad \lambda_0 = \frac{c_0}{f_0}$$

$$\Rightarrow f_0 = \frac{3 \cdot 10^8}{102,65 \cdot 10^{-3}} = 2,92 \text{ GHz} \quad (3 \text{ GHz facit})$$

c)



$$\lambda = 74,4 \text{ mm}$$

$$d_s = 24,5 \text{ mm}$$

$$\frac{24,5}{74,4} = 0,33$$

$$\Rightarrow d_s = 0,33 \lambda$$

$$\frac{l_s}{\lambda} = \frac{2,8}{74,4} = 0,04 \Rightarrow l_s = 0,04 \lambda \quad (0,038 \lambda \text{ facit})$$

helt ok

$$S.D \Rightarrow \Gamma_s = 0,9 \angle -94^\circ$$

$$l_d = 0,134 \lambda$$

$$S.D \Rightarrow \Gamma_L = 0,5 \angle -180^\circ$$

$$d_d = 0,082 \lambda$$

samma för Γ_L

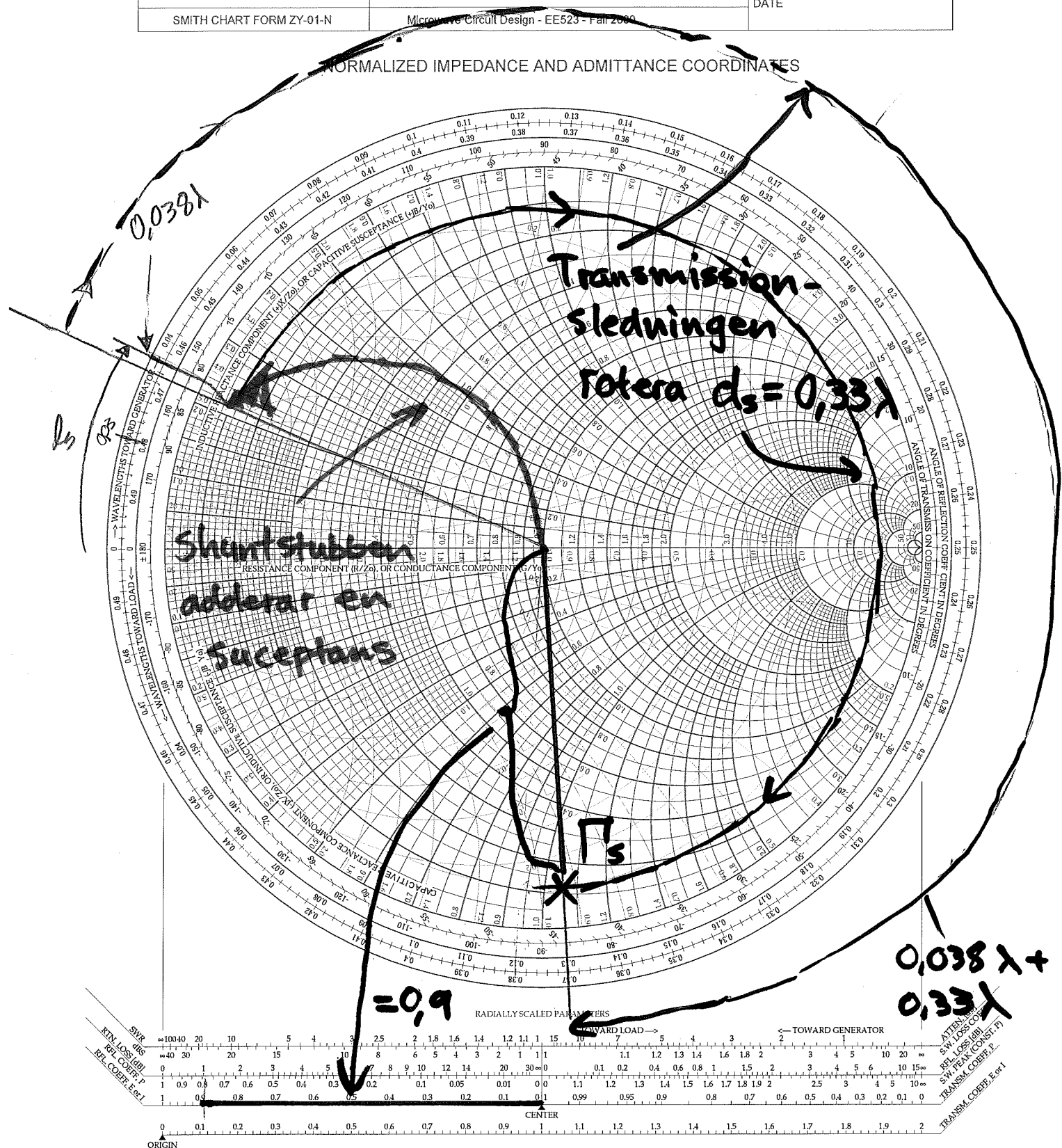
se även lösning i facit

Tenta 170411 2c

Γ_s

NAME	TITLE	DWG. NO.
SMITH CHART FORM ZY-01-N	Microwave Circuit Design - EE523 - Fall 2000	DATE

NORMALIZED IMPEDANCE AND ADMITTANCE COORDINATES



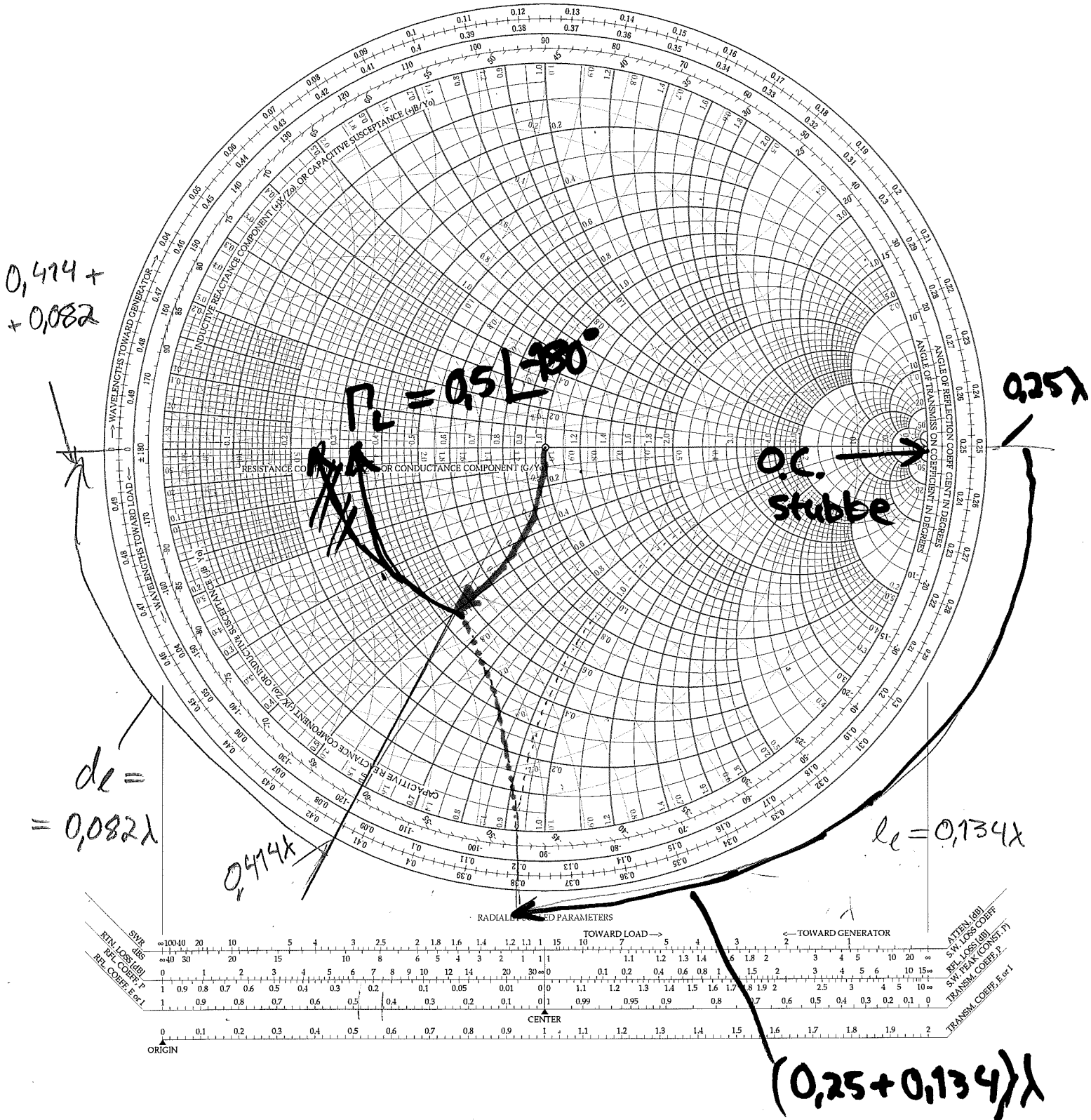
$$\Gamma_s = 0.9 \angle -87^\circ$$

Tenta 170411 2c

Γ_L

NAME	TITLE	DWG. NO.
SMITH CHART FORM ZY-01-N	Microwave Circuit Design - EE523 - Fall 2000	DATE

NORMALIZED IMPEDANCE AND ADMITTANCE COORDINATES



$$\Gamma_L = 0.5 \angle -180^\circ$$